

# Fractions

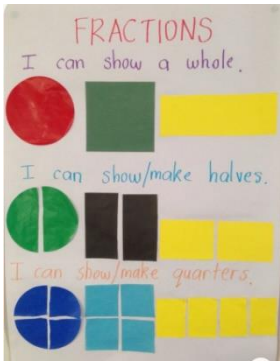
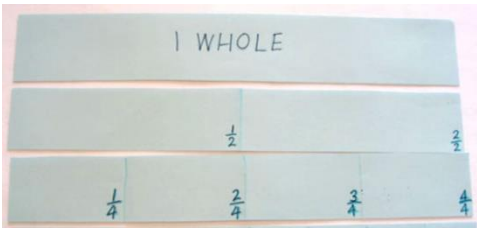



## Foundation Stage Objectives:

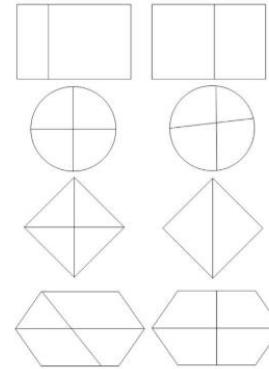
- Solve practical problems involving sharing and halving. **See Division section of policy.**

## Year 1 Objectives:

- Recognise, find and name a half as one of two equal parts of an object, shape or quantity.
- Recognise, find and name a quarter as one of four equal parts of an object, shape or quantity.

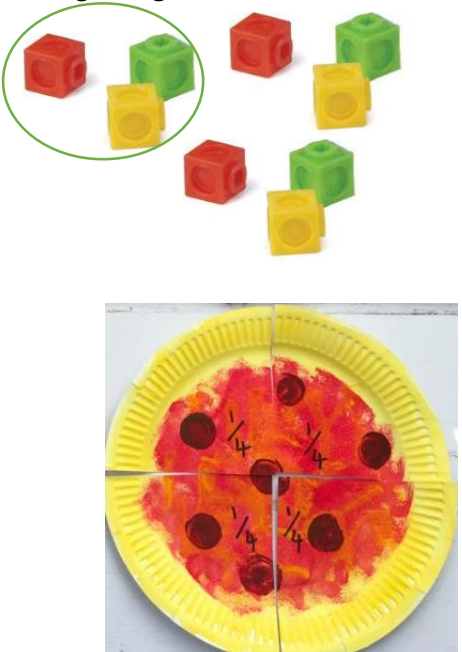
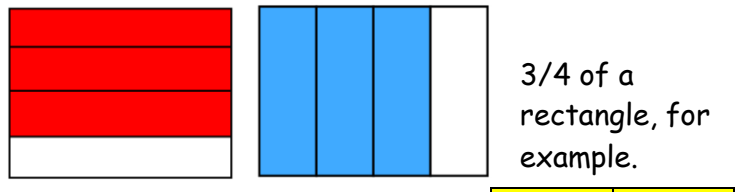
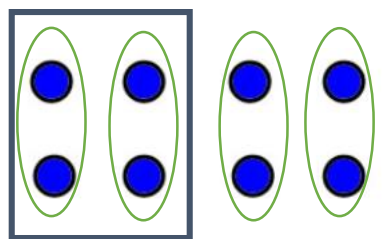
Concrete	Pictorial	Abstract
<p>Pupils will use practical objects, including within their role play and outside areas to find <math>\frac{1}{2}</math> and <math>\frac{1}{4}</math> of different amounts and shapes.</p>		
<p>Bar Model using strips of paper, I find <math>\frac{1}{2}</math> and <math>\frac{1}{4}</math> by folding and cutting different sizes and shapes in order to support their understanding of fractions.</p>  	<p>E.g. find half (<math>\frac{1}{2}</math>) of the items on each picture or shape. Do the same for a quarter (<math>\frac{1}{4}</math>).</p> 	<p>Half of 10 = 5  <math>\frac{1}{2}</math> of 6 = 3</p> <p>A quarter of 20 =  <math>\frac{1}{4}</math> of 8 = 2</p>

Repeat with shapes: Which have been cut exactly into quarters?



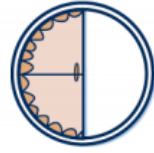
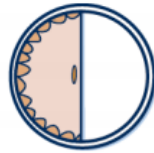
**Year 2 Objectives:**

- Recognise, find, name and write fractions  $1/3$  ,  $1/4$  ,  $2/4$  and  $3/4$  of a length, shape, set of objects or quantity
- Write simple fractions for example,  $1/2$  of  $6 = 3$  and recognise the equivalence of  $2/4$  and  $1/2$  .

Concrete	Pictorial	Abstract
<p>Recognising <math>1/3</math>, <math>1/4</math>, <math>2/4</math> and <math>3/4</math></p> 	<p>Find different ways of finding fractions of shapes</p>  <p><math>3/4</math> of a rectangle, for example.</p> <p><math>2/4</math> of a quantity. <math>2/4</math> of <math>8 = 4</math></p> 	<p><math>1/3</math> of <math>9 = 3</math></p> <p><math>2/4</math> of <math>8 = 4</math></p> <p><math>3/4</math> of <math>12 = 9</math></p>

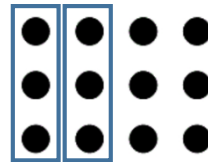
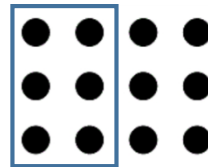
Recognise equivalence.

$$\frac{1}{2} = \frac{2}{4}$$



$\frac{2}{4}$  of a pie =  $\frac{1}{2}$  of a pie

$\frac{1}{2}$  of 12 =  $\frac{2}{4}$  of 12



$$\frac{1}{2} \text{ of } 12 = 6$$

$$\frac{2}{4} \text{ of } 12 = 6$$

### Year 3 Objectives:

- Recognise and show, using diagrams, equivalent fractions with small denominators
- Recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators
- Add and subtract fractions with the same denominator within one whole [for example,  $\frac{5}{7} + \frac{1}{7} = \frac{6}{7}$ ]
- Solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole number

Recognise and show equivalent fractions using fraction bars/strips, for example



$\frac{1}{2}$



$\frac{2}{4}$



$\frac{3}{6}$



$\frac{4}{8}$

David says two sixths is the same as one third. Is he correct? How do you know?

Fractions of a discrete set of objects.

Unit fraction  $\frac{1}{8}$

$$\frac{1}{5} \text{ of } 15 \text{ sweets} = 3$$
$$(15 \div 5 = 3)$$



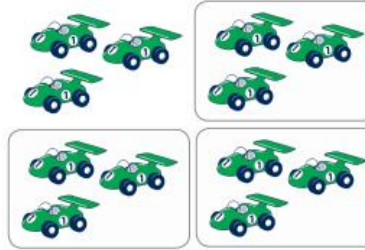
Non-unit fraction 3/7



1/8

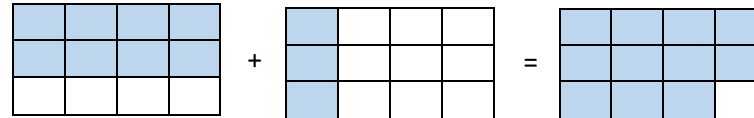


3/4



2/5 of 15 sweets = 6  
(15 ÷ 5 = 3 and 3 × 2 = 6)

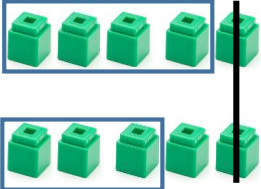
Add and subtract fractions with the same denominator within 1 whole.



$$8/12 + 3/12 = 11/12$$

Comparing the two fractions and finding the difference/

$$4/5 - 3/5 = 1/5$$



$$4/5 - 3/5 = 1/5$$


Solve problems:

David spent 1/4 of his money on a book. The book cost £10. How much money did he start off with?

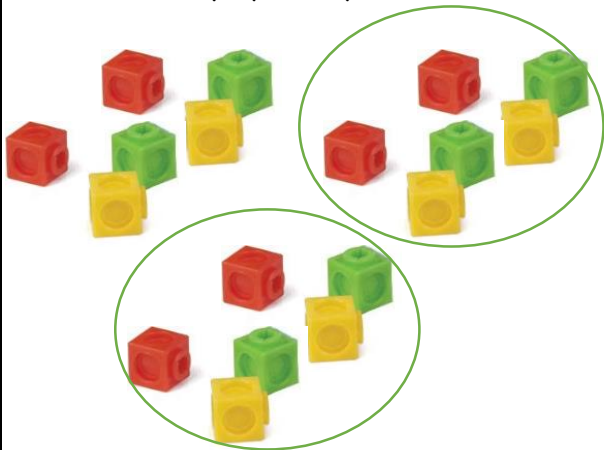
$$1/4 = £10$$

$$4 \times £10 = £40$$

Total Money?			
1/4	1/4	1/4	1/4

	<table border="1" style="width: 100%; text-align: center;"> <tr> <td style="background-color: #f4b084;">£10</td> <td style="color: red;">£10</td> <td style="color: red;">£10</td> <td style="color: red;">£10</td> </tr> </table>	£10	£10	£10	£10	
£10	£10	£10	£10			
Concrete	Pictorial	Abstract				
<b>Year 4 Objectives:</b> <ul style="list-style-type: none"> <li>• Add and subtract fractions with the same denominator</li> <li>• Solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole number</li> </ul>						
Concrete	Pictorial	Abstract				
<p>Adding and subtracting fractions as above</p> <p>Solve problems including non-unit fractions</p>	<p><math>2/3</math> of £18 =</p> 	<p><math>3/8 + 5/8 = 8/8</math> (same as 1 whole)</p> <p><math>6/7 - 4/7 = 2/7</math></p> <p><math>2/3</math> of £18 =  <math>£18 \div 3 = £6</math>  <math>£6 \times 2 = £12</math></p>				

Use counters/play money to find  $\frac{2}{3}$ .



**Year 5 Objectives:**

- Add and subtract fractions with the same denominator and denominators that are multiples of the same number
- Recognise mixed numbers and improper fractions and convert from one form to the other and write mathematical statements  $> 1$  as a mixed number [for example,  $\frac{2}{5} + \frac{4}{5} = \frac{6}{5} = 1 \frac{1}{5}$ ]
- Multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams

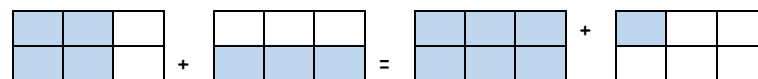
**Concrete**

Add and subtract fractions with same denominator and denominators that are multiples of the same number, and recognise mixed numbers and improper fractions.

$$\frac{2}{3} + \frac{2}{3} = \frac{4}{3} = 1 \frac{1}{3}$$



**Pictorial**



$$\frac{4}{6} + \frac{3}{6} = 1 \text{ whole} + \frac{1}{6} \quad (\frac{7}{6})$$



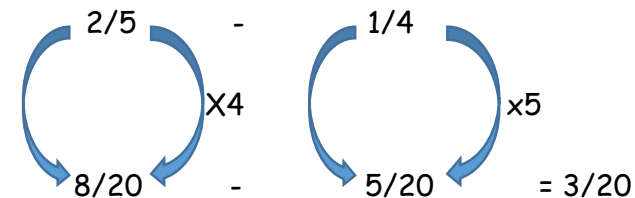
$$\begin{array}{r} \frac{2}{5} \\ \frac{8}{20} \end{array} - \begin{array}{r} \frac{1}{4} \\ \frac{5}{20} \end{array} = \frac{3}{20}$$


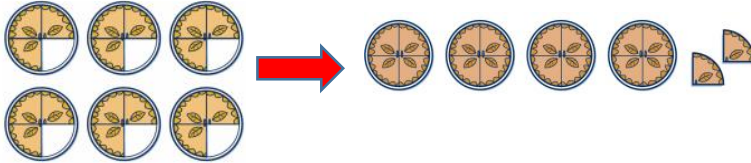
**Abstract**

$$\frac{4}{6} + \frac{3}{6} = \frac{7}{6} = 1 \frac{1}{6}$$

$$1 \frac{1}{6} = \frac{7}{6} \text{ (because } 1 = \frac{6}{6}\text{)}$$

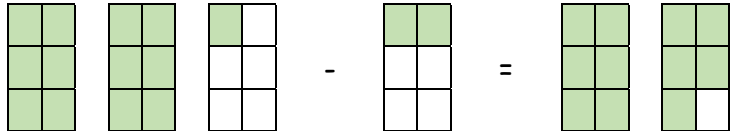
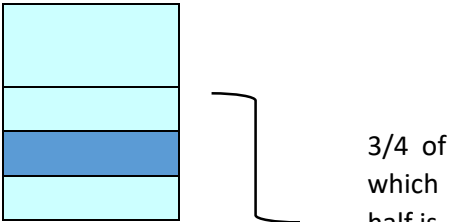

$$\frac{2}{5} - \frac{1}{4} =$$



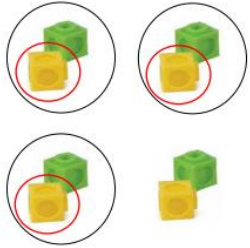
<p>Multiply proper fractions and mixed numbers by a whole number  <math>6 \times 3/4</math></p> 	<p><math>6 \times 3/4 = 4 \frac{2}{4}</math></p> 	<p><math>6 \times 3/4 = 18/4 = 4 \frac{2}{4}</math> or <math>4 \frac{1}{2}</math></p>
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**Year 6 Objectives:**

- Add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions
- Multiply simple pairs of proper fractions, writing the answer in its simplest form [for example,  $1/4 \times 1/2 = 1/8$  ]
- Divide proper fractions by whole numbers [for example,  $1/3 \div 2 = 1/6$  ]

Concrete	Pictorial	Abstract
<p>Add and Subtract fractions - as year 5</p> <p>With mixed numbers</p>	<p><math>2 \frac{1}{6} - 1/3</math></p>  <p><math>2 \frac{1}{6} - 1/3 = 1 \frac{5}{6}</math></p>	<p><math>2 \frac{1}{6} - 1/3</math> (find the same denominator)</p> <p><math>2 \frac{1}{6} - 2/6</math> ( change 1 whole into a fraction and add to the existnig fraction)</p> <p><math>1 \frac{7}{6} - 2/6 = 1 \frac{5}{6}</math></p>
<p>Multiply simple pairs of proper fractions.</p>	<p><math>1/2 \times 3/4</math></p>  <p>3/4 of which half is shaded</p>	<p><math>1/2 \times 3/4 = 3/8</math></p> <ol style="list-style-type: none"> <li>1. Multiply the numerator.</li> <li>2. Multiply the denominator.</li> <li>3. Simplify where possible.</li> </ol> 

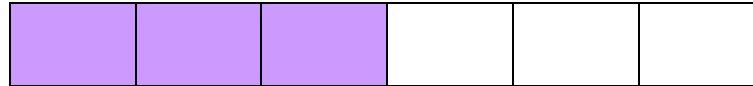
$$\frac{1}{2} \times \frac{3}{4} = \frac{3}{8}$$



$$\frac{2}{5} \times \frac{5}{6} = \frac{10}{30} = \frac{1}{3}$$
A blue curved arrow pointing from the 5 in the denominator of the first fraction to the 5 in the numerator of the second fraction, with an 'x' below it.

Divide proper fractions by whole numbers

$$\frac{1}{2} \div 3 =$$



$$\frac{1}{2} \div 3 = \frac{1}{6}$$